

Resolution Enhancement of Images Using DTCWT and NLM

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Abstract—Resolution enhancement (RE), a process of improving the quality of an image. Resolution enhancement is basically obtained by regaining high frequency contents of image. Without which the output will be a blurred image. In this paper a new approach in wavelet domain using dual-tree complex wavelet transform (DT-CWT) and nonlocal means (NLM) filter for RE of the images is implemented. An input image is decomposed by DT-CWT to obtain high-frequency sub bands. The high-frequency sub bands and the low-resolution (LR) input image will be interpolated using the bicubic interpolation in proposed work. The high frequency sub bands are passed through an NLM filter to reduce the artifacts generated by DT-CWT. The filtered high-frequency sub bands and the LR part of input image are added using inverse DTCWT for obtaining resolution-enhanced image. DT-CWT provides superior resolution and greater performance ratio because of its nearly shift invariant and directional selective properties. The results are compared in terms of PSNR, MSE for existing techniques.

IndexTerms—DT-CWT, Bicubic interpolation, RE, NLM, PSNR

I. INTRODUCTION

Resolution is the quality of an image. Three types of resolutions which affect quality of image spatial, spectral, and temporal. So for improving quality of image resolution enhancement (RE) is desirable. For resolution enhancement, interpolation is widely used [2], [3]. Some of the commonly used interpolation techniques are nearest neighbor, bilinear, bicubic.

RE schemes not using wavelets suffer from blurring of an image because of loss of high-frequency contents. That would have been the major drawback for RE schemes. So therefore new approach has been started in the wavelet domain. In recent years many algorithms such as DWT [7], SWT [8], and DT-CWT [9] have been proposed. There are some conventional schemes such as nearest neighbor, bilinear, and bucolic interpolations and wavelet zero padding, this RE scheme using DT-CWT and bicubic interpolations were compared with conventional schemes [9].

Note that, artifacts in RE image causes due to property of shift variant and lack of directionality of DWT. In case of DT-CWT; it is almost shift invariant and directional selective [13].

In this paper, DT-CWT-NLM-RE technique is used by additional use of bicubic interpolation. Note that Perfect reconstruction can be achieved by help of DT-CWT with well-balanced frequency responses [13] [14].

DT-CWT is more advantageous than traditional DWT because it gives more promising results after the modifying the wavelet coefficients. Since the bicubic interpolation offer less aliasing, sharpness, and minimal ringing, it is therefore a good choice for RE. For further enhancement of performance of DT-CWT-NLM-RE NLM filtering [15] which reduces the artifacts. The results for this method are compared with the best performing RE techniques [5], [7]–[9].

II. NON LOCAL MEAN FILTER

The NLM filter is an improved version of neighborhood filtering algorithms. Basically assumption is that, an image content repeat itself in within some neighborhood [15] and in neighboring frames [16]. In NLM weighted sum of the surrounding pixels $Y(p, q)$ (same frame and in the neighboring frames [16]) is taken which helps to compute denoised pixel $x(p, q)$. In noise contaminated images this feature helps to calculate the pixel value. To calculate the denoised pixel $x(p, q)$ following formula can be used [1]

$$x(p, q) = \frac{\sum_{m=1}^M \sum_{(r,s) \in N(p,q)} Y_m(r,s) K_m(r,s)}{\sum_{m=1}^M \sum_{(r,s) \in N(p,q)} K_m(r,s)} \quad (1)$$

where m denotes frame index, and N indicate the neighborhood of the pixel at pixel (p, q) . K is the filter weights, i.e.

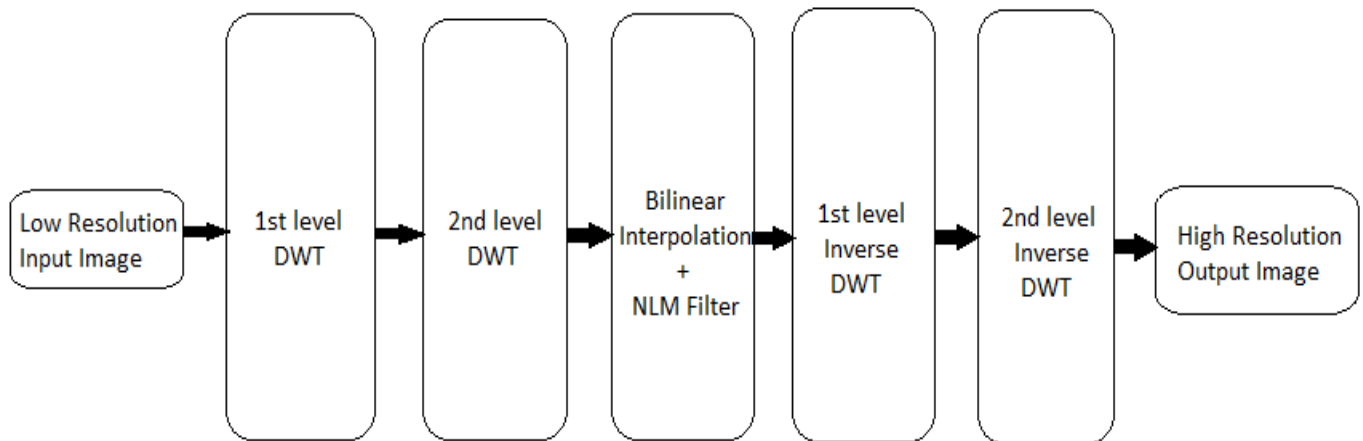


Fig 1. Block diagram of DTCWT-NLM-RE

$$K(r, s) = \frac{\exp\left\{-\frac{\|V(p, q) - V\|_2^2}{2\sigma^2}\right\}}{X \sqrt{(p-r)^2 + (q-s)^2 + (m-1)^2}} \quad (2)$$

where V is centered at $Y(p, q)$ pixel which makes the squared window. $Y(r, s)$ are the pixel values from a geometric neighborhood of pixels $Y(p, q)$ and $Y(r, s)$, σ is the filter coefficient, and $f(x)$ is a geometric distance function, distance between $Y(p, q)$ and $Y(r, s)$ is inversely proportional to the filter weight K .

B. NLM-RE

Resolution enhancement is done by modifying NLM with the following model [17]:

$$L_m = IJQX + n \quad (3)$$

where L_m is the vectorized low-resolution frame, I denotes decimation operator, J denotes blurring matrix, Q denotes warping matrix, X denotes vectorized high-resolution image, and n is Gaussian white noise. Series of L is formed here and aim is to restore X from it. Penalty function ϵ is defined as

$$\epsilon^2 = \frac{1}{2} \sum_{m=1}^M \|IJQx - Y_m\|_2^2 + \lambda R(x) \quad (4)$$

where R is a regularization term. λ is the scale coefficient. x is the target image, and Y_m represents low resolution input image. In [17], the total variation kernel is taken to replace R ,

which is an image deblurring kernel. To simplify the algorithm, problem in (4) is separated by minimizing

$$\epsilon_{fusion}^2(Z) = \frac{1}{2} \sum_{m=1}^M (IQZ - L_m)^T O_m (IQZ - L_m) \quad (5)$$

where the blurred version of the target image denoted by Z and O_m is the weight matrix, followed by minimizing a deblurring equation [11], i.e.

$$\epsilon_{RE}^2(X) = \|JX - Z\|_2^2 + \lambda R(Z) \quad (6)$$

A pixel wise solution of equation (5) can be obtained as

$$\hat{Z} = \frac{\sum_{m=1}^M \sum_{(r,s) \in N(p,q)} Y_m^r(r,s) K_m^r(r,s)}{\sum_{m=1}^M \sum_{(r,s) \in N(p,q)} K_m^r(r,s)} \quad (7)$$

where the superscript r refers to the High Resolution (HR) coordinate. Instead of calculating the target pixel position in neighborhood frames, the algorithm estimates all possible pixel positions; therefore, motion estimation is avoided [11]. Equation (7) apparently resembles (1), but (7) has some differences as compared with (1). The weight estimation in (2) should be modified because size of high resolution image and K 's corresponding matrix O must have to be of the same size. Therefore, before computing K a simple upscaling process is needed for patching V . The total number of pixel Y in (7) should be equal to the number of weights K .

Thus, a zero-padding interpolation is applied to L before fusing the images [11].

III. PROPOSED TECHNIQUE

In the proposed algorithm (DT-CWT-NLM-RE) [1], decomposition of the LR input image in different subbands (i.e., C_i and W_i^j , where $i \in \{A, B, C, D\}$ and $j \in \{1, 2, 3\}$) by using DT-CWT, as shown in Fig. 1. C_i denotes the image coefficient subbands values, and W_i^j denotes wavelet coefficient subbands values. The subscript A denotes the even-row and even-column index, B denotes the odd-row and even column index, C denotes the even-row and odd-column index, and D denotes odd-row and odd-column index, whereas h represent the low-pass and g represent the high-pass filters. The superscript e for even and o for odd indices.

W_i^j values are interpolated by factor β using the bicubic interpolation and combined with the $\beta/2$ -interpolated low resolution input image. Since C_i contains low-pass-filtered image losing high-frequency information of the LR input image. So for that we have used the low resolution input image instead of C_i . Although the DT-CWT is having the property of shift invariance [14], however, it may produce artifacts after the interpolation of W_i^j . Therefore, to reduce these artifacts, NLM filtering is used.

All interpolated W_i^j values are passed through the NLM filter. Then; we apply the inverse DT-CWT decomposition to these filtered subbands along with the interpolated low resolution input image to reconstruct the high resolution image. The results will show better performance of proposed DT-CWT-NLM algorithm by comparing PSNR, and MSE [18].

IV. RESULTS

There are majorly two commonly used measures: Mean-Squared Error and Peak Signal-to-Noise Ratio. The mean-squared error (MSE) between two images $g(x,y)$ and $\hat{g}(x,y)$ is given by:

$$e_{MSE} = \frac{1}{MN} \sum_{n=1}^M \sum_{m=1}^N [\hat{g}(n, m) - g(n, m)]^2 \quad (8)$$

Peak Signal-to-Noise Ratio (PSNR) is given by:

$$PSNR = -10 \log_{10} \frac{e_{MSE}}{S^2} \quad (9)$$

where S is the maximum pixel value. PSNR is measured in decibels (dB).

The image of Washington DC Digital Aerial Photography -0.15 mis taken here for comparison with existing RE techniques. Here by down sampling the original HR image by a factor of 4, the input LR image is obtained. Results are shown in fig. (2)

TABLE I
COMPARISON OF THE EXISTING AND PROPOSED TECHNIQUES FOR THE "WASHINGTON DC" IMAGE

ALGORITHM	MSE	PSNR(dB)
SWT-RE[8]	0.0464	13.3332
DWT-RE[7]	0.0419	13.7802
SWT-DWT-RE[8]	0.0335	14.7527
VVIR-PDE-RE[5]	0.0269	15.6970
DT-CWT-RE[9]	0.0242	16.1576

V. CONCLUSION

An RE technique based on DT-CWT, bicubic interpolator and Non Local Mean filter has been modified. In this technique DT-CWT decomposes the input LR image. DT-CWT is used instead of DWT since it is almost shift invariant and produce fewer artifacts than DWT. Bicubic interpolator interpolates wavelet coefficients and the LR input image. NLM filtering here used to overcome the artifacts generated by decomposition due to DT-CWT and for the further enhancement of performance is compared in terms of PSNR, MSE for the proposed technique. Hence this technique will give better results than the conventional algorithms.

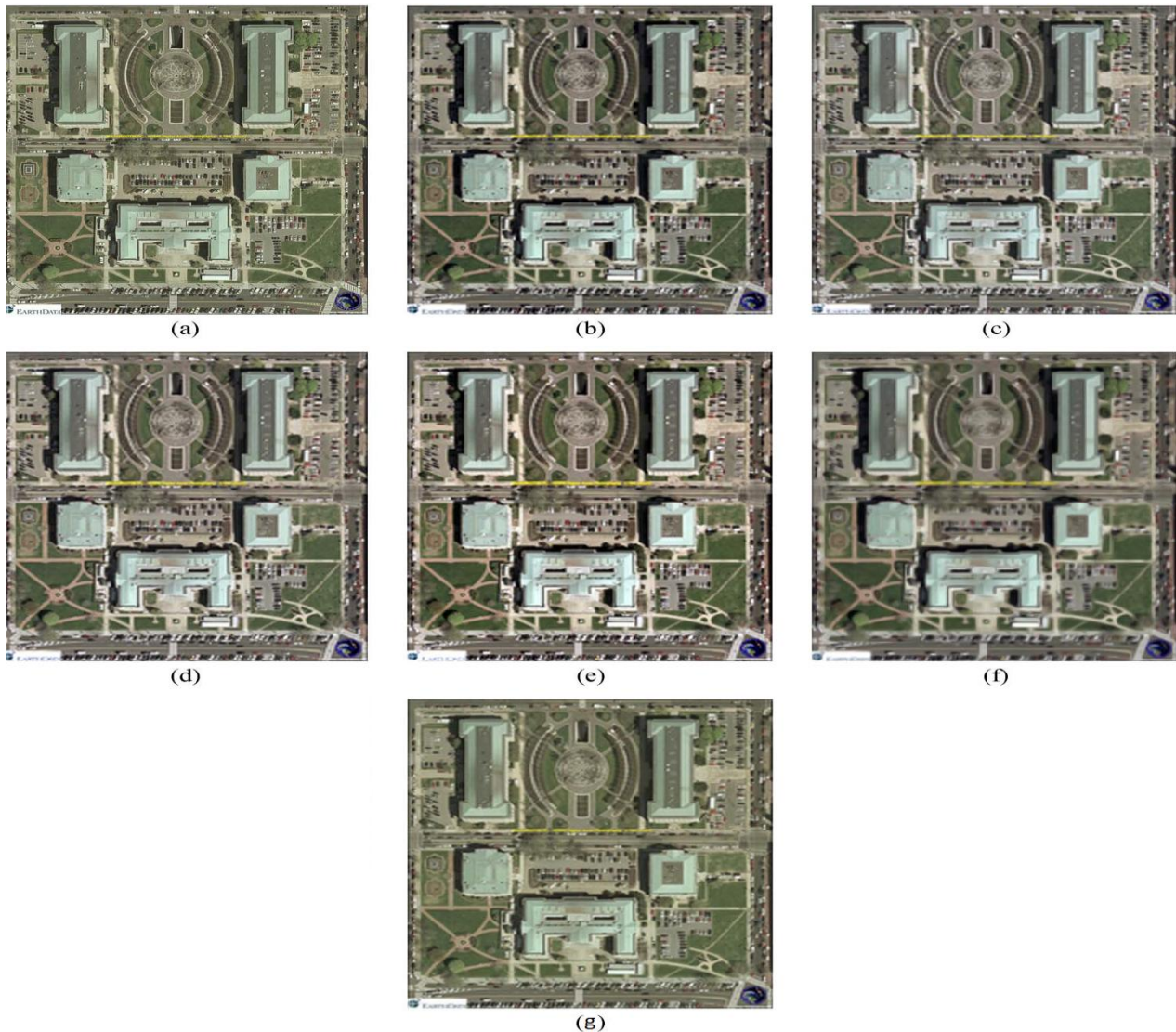


Fig. 2. (a) Original “Washington DC” image. (b) Input image. (c) SWT-RE. (d) DWT-RE. (e) SWT-DWT-RE. (f) VVIR-PDE-RE. (g) DT-CWT-RE

REFERENCES

- [1] Muhammd Zafar Iqbal, Abdul Ghafor, And AdilMasoodSiddiqui, “*Satellite Image Resolution Enhancement Using Dual-Tree Complex Wavelet Transform And Nonlocal Means*” Ieee Geoscience And Remote Sensing Letters, Vol. 10, No. 3, May 2013
- [2] Y. Piao, I. Shin, and H. W. Park, “*Image resolution enhancement using inter-subband correlation in wavelet domain,*” in *Proc. Int. Conf. ImageProcess.*, San Antonio, TX, 2007, pp. I-445–I-448.
- [3] C. B. Atkins, C. A. Bouman, and J. P. Allebach, “*Optimal image scaling using pixel classification,*” in *Proc. Int. Conf. Image Process.*, Oct. 7–10,2001, pp. 864–867.
- [4] A. S. Glassner, K. Turkowski, and S. Gabriel, “*Filters for common resampling tasks,*” in *Graphics Gems*. New York: Academic, 1990,pp. 147–165.
- [5] D. Tschumperle and R. Deriche, “*Vector-valued image regularization with PDE’s: A common framework for different applications,*”*IEEETrans.Pattern Anal. Mach. Intell.*, vol. 27, no. 4, pp. 506–517, Apr. 2005.
- [6] M. J. Fadili, J. Starck, and F. Murtagh, “*Inpainting and zooming using sparse representations,*”*Comput. J.*, vol. 52, no. 1, pp. 64–79, Jan. 2009.
- [7] H. Demirel and G. Anbarjafari, “*Discrete wavelet transform-based satellite image resolution enhancement,*”*IEEE Trans. Geosci. Remote Sens.*,vol. 49, no. 6, pp. 1997–2004, Jun. 2011.

- [8] H. Demirel and G. Anbarjafari, "Image resolution enhancement by using discrete and stationary wavelet decomposition," *IEEE Trans. Image Process.*, vol. 20, no. 5, pp. 1458–1460, May 2011.
- [9] H. Demirel and G. Anbarjafari, "Satellite image resolution enhancement using complex wavelet transform," *IEEE Geosci. Remote Sens. Lett.*, vol. 7, no. 1, pp. 123–126, Jan. 2010.
- [10] H. Demirel and G. Anbarjafari, "Image super resolution based on interpolation of wavelet domain high frequency subbands and the spatial domain input image," *ETRI J.*, vol. 32, no. 3, pp. 390–394, Jan. 2010.
- [11] H. Zheng, A. Bouzerdoum, and S. L. Phung, "Wavelet based non-local means super-resolution for video sequences," in *Proc. IEEE 17th Int. Conf. Image Process.*, Hong Kong, Sep. 26–29, 2010, pp. 2817–2820.
- [12] A. Gambardella and M. Migliaccio, "On the superresolution of microwave scanning radiometer measurements," *IEEE Geosci. Remote Sens. Lett.*, vol. 5, no. 4, pp. 796–800, Oct. 2008.
- [13] I. W. Selesnick, R. G. Baraniuk, and N. G. Kingsbur, "The dual-tree complex wavelet transform," *IEEE Signal Process. Mag.*, vol. 22, no. 6, pp. 123–151, Nov. 2005.
- [14] J. L. Starck, F. Murtagh, and J. M. Fadili, "Sparse Image and Signal Processing: Wavelets, Curvelets, Morphological Diversity" Cambridge, U.K.: Cambridge Univ. Press, 2010.
- [15] A. Buade, B. Coll, and J. M. Morel, "A review of image denoising algorithms, with a new one," *Multisc. Model. Simul.*, vol. 4, no. 2, pp. 490–530, 2005.
- [16] A. Buades, B. Coll, and J. M. Morel, "Denoising image sequences does not require motion estimation," in *Proc. IEEE Conf. Audio, Video Signal Based Surv.*, 2005, pp. 70–74.
- [17] M. Protter, M. Elad, H. Takeda, and P. Milanfar, "Generalizing the nonlocal-means to super-resolution reconstruction," *IEEE Trans. Image Process.*, vol. 18, no. 1, pp. 36–51, Jan. 2009.
- [18] Z. Wang and A. C. Bovik, "A universal image quality index," *IEEE Signal Process. Lett.*, vol. 9, no. 3, pp. 81–84, Mar. 2002.
- [19] [Online]. Available: <http://www.satimagingcorp.com/>

