

A Novel Approach For the Design and Implementation of FPGA Based High Speed Digital Modulators Using Cordic Algorithm

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Abstract— The main objective of this paper is to implement all digital modulation techniques into a single module and implement in a Field Programmable Gate Array (FPGA). The proposed system allows the user to select any one of four modulations without reconfiguring the FPGA. Carrier waveform for the modulator is generated using coordinate rotation digital computer CORDIC algorithm which uses shift, addition and very small look up table (LUT). It is hardware efficient and iterative algorithm for circular rotation and an efficient method to compute trigonometric functions. The codes for these digital modulators are developed in VHDL and the functionality of these digital modulators was simulated using the MODELSIM simulation software and synthesized by Xilinx ISE Design suite14.5 and finally implemented in SPARTAN-3E FPGA.

Index Terms— Binary amplitude shift keying (BASK) , Binary phase shift keying (BPSK), Binary frequency shift keying (BFSK), Quadrature phase shift keying (QPSK) ,Field Programmable Gate Array,(FPGA),CORDIC

I. INTRODUCTION

This paper describes a method to implement all modulation technique (BASK, BPSK, BFSK, QPSK) on field programmable gate array (FPGA) development board which is widely available and inexpensive. In the existing system^[1], BASK, BFSK, BPSK modulation techniques are only discussed. In the proposed system we can include QPSK along with other modulation techniques. Also in this paper CORDIC algorithm is used to design carrier waveforms. It is commonly used when no hardware multiplier is available (e.g., simple micro controllers and FPGAs) as the only operations it requires are addition, subtraction, bit shift and lookup table. The CORDIC algorithm provides an iterative method of performing vector rotations by arbitrary angles using only shifts and adds. CORDIC can be used to calculate the sine and cosine of an angle, and assumes the desired angle is given in radians and represented in a fixed-point format. To determine the sine or cosine for an angle β , the y or x coordinate of a point on the unit circle corresponding to the desired angle must be found. Using CORDIC, we would start with the vector v_0 , where $v_0 = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$

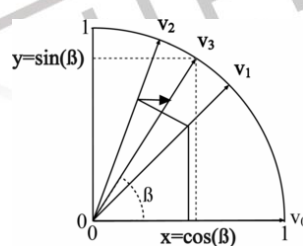


Fig. 1. CORDIC principle

In the first iteration, this vector is rotated 45° counterclockwise to get the vector. Successive iterations rotate the vector in one or the other direction by size-decreasing steps, until the desired angle has been achieved. Step size denoted by i is $\arctan(1/(2^i-1))$ for $i = 1, 2, 3$, every iteration calculates a rotation, which is performed by multiplying the vector with the rotation matrix R_i $V_i = V_{i-1} R_i$.

The rotation matrix is given by:

$$R_i = \begin{bmatrix} \cos \gamma_i & -\sin \gamma_i \\ \sin \gamma_i & \cos \gamma_i \end{bmatrix} \quad (1)$$

Using the following two trigonometric identities:

$$\cos \alpha = \frac{1}{\sqrt{1+\tan^2 \alpha}} \quad (2)$$

$$\sin \alpha = \frac{\tan \alpha}{\sqrt{1+\tan^2 \alpha}} \quad (3)$$

The rotation matrix becomes:

$$R_i = \frac{1}{\sqrt{1+\tan^2 \gamma_i}} \begin{bmatrix} 1 & -\tan \gamma_i \\ \tan \gamma & 1 \end{bmatrix} \quad (4)$$

The expression for the rotated vector becomes:

$$V_i = \frac{1}{\sqrt{1+\tan^2 \gamma_i}} \begin{bmatrix} 1 & -\tan \gamma_i \\ \tan \gamma & 1 \end{bmatrix} \begin{bmatrix} x_{i-1} \\ y_{i-1} \end{bmatrix} \quad (5)$$

The expression becomes:

$$V_i = K_i \begin{bmatrix} 1 & -\alpha_i 2^{-i} \\ \sigma_i 2^{-i} & 1 \end{bmatrix} \begin{bmatrix} x_{i-1} \\ y_{i-1} \end{bmatrix} \quad (6)$$

Where

$$K_i = \frac{1}{\sqrt{1+2^{-2i}}}$$

And can have the values of -1 or 1 , and is used to determine the direction of the rotation; if the angle is positive then is $+1$, otherwise it is -1 .

$$K(n) = \prod_{i=0}^{n-1} K_i = \prod_{i=0}^{n-1} \frac{1}{\sqrt{1+2^{-2i}}} \quad (7)$$

Which is calculated in advance and stored in a table, or as a single constant if the number of iterations is fixed. This correction could also be made in advance, by scaling and hence saving a multiplication.

II. DIGITAL MODULATORS

A. BPSK

In BPSK we change the phase of the sinusoidal carriers to indicate information. Phase in this context is the starting angle at which sinusoid starts. To transmit 0, we shift the phase of the sinusoid by 180° as shown in Fig. 2. Phase shift represents the change in the state of the information. In this case

$$S(t) = A_c \sin(2\pi fct) ; \text{ if symbol } = 1$$

$$S(t) = -A_c \sin(2\pi fct) ; \text{ if symbol } = 0$$

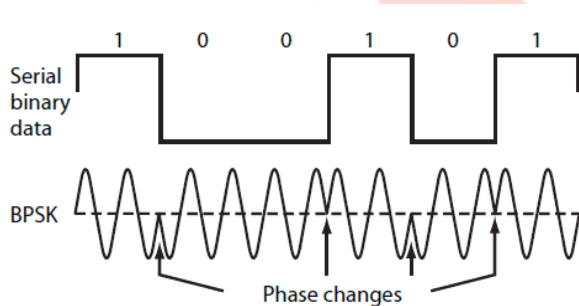


Fig. 2. BPSK modulation

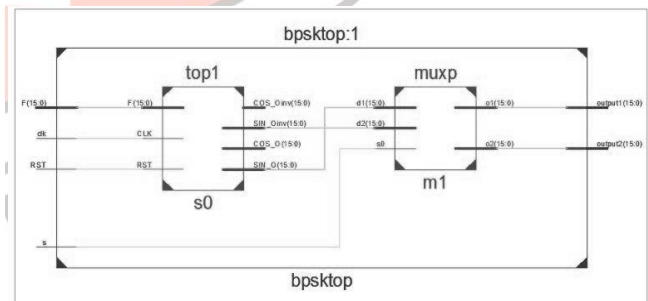


Fig. 3. Block diagram for BPSK

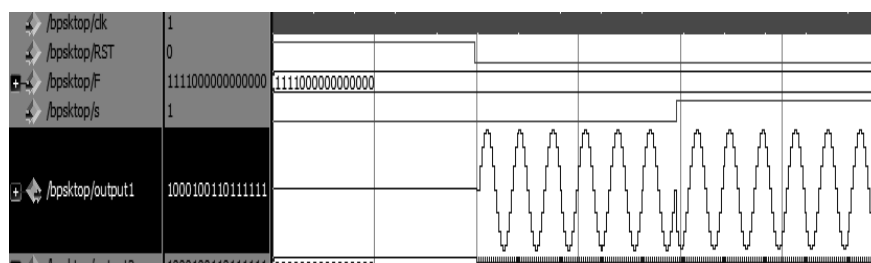


Fig. 4. Simulation result for BPSK modulation

B. BASK

In BASK, the amplitude of the signal is changed in response to information and all else is kept fixed. Bit 1 is transmitted by a signal of one particular amplitude. To transmit 0, we change the amplitude keeping the frequency constant. On-Off Keying (OOK) is a special form of ASK, where one of the amplitude is zero as shown in Fig. 5 below. BASK signal can be represented as

$$S(t) = A_c \sin(2\pi fct) ; \text{ if symbol } = 1$$

$$S(t) = 0 ; \text{ if symbol } = 0$$

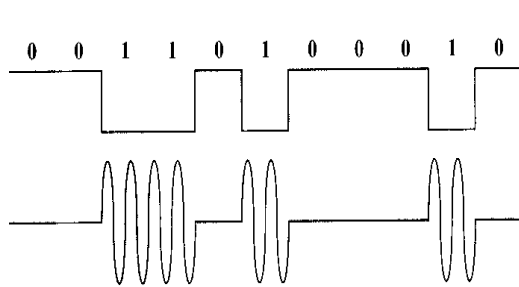


Fig. 5. BASK modulation

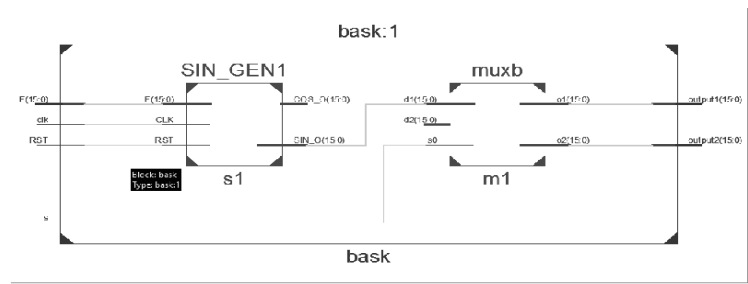


Fig. 6 . Block diagram for BASK modulation

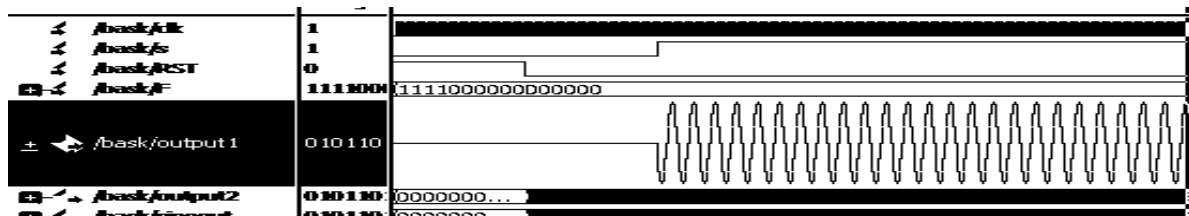


Fig. 7. Simulation result for BASK modulation

C. BFSK

In FSK, we change the frequency in response to information, one particular frequency for a 1 and another frequency for a 0 as shown in Fig.8. In the example frequency f_1 for bit 1 is higher than f_2 used for a 0 bit. In general it is called m-array FSK. When m is two then it is called binary –FSK with two carriers. A BFSK signal is represented as

$$S(t) = A_c \sin(2\pi f_1 t) ; \text{ if symbol} = 1$$

$$S(t) = A_c \sin(2\pi f_2 t) ; \text{ if symbol} = 0$$

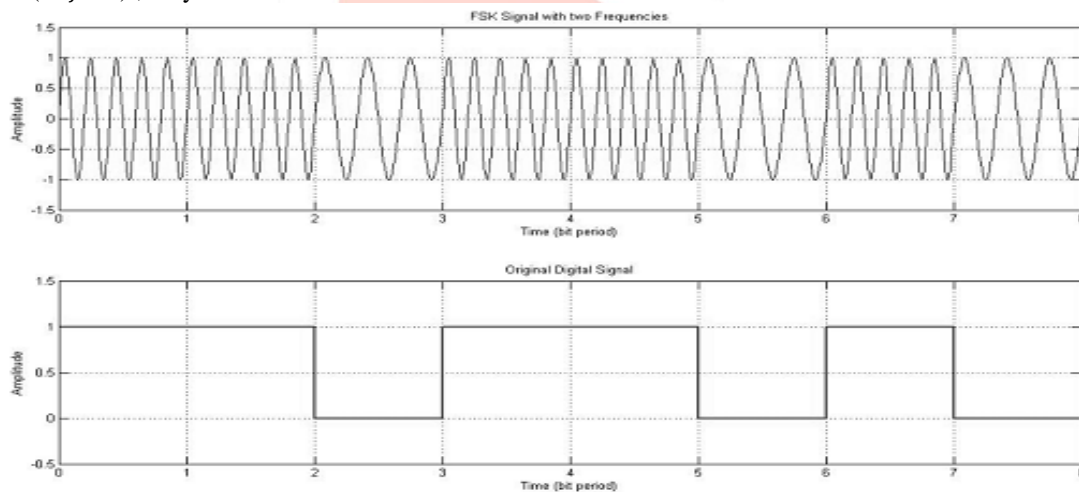


Fig.8. BFSK modulation

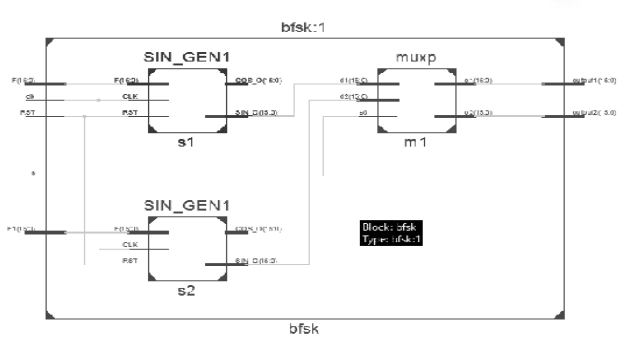


Fig .9. Block diagram for BFSK modulation

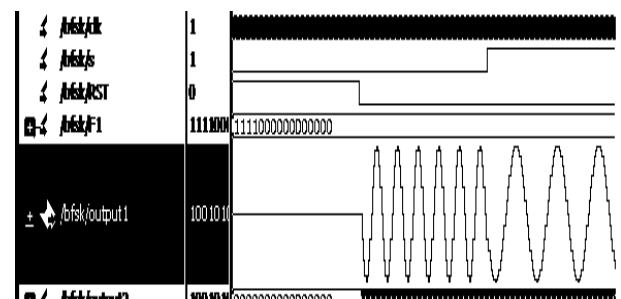
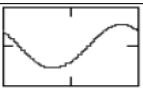
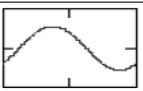
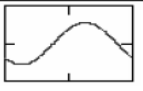
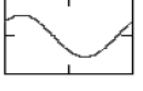


Fig.10. Simulation result for BFSK modulation

D. QPSK

QPSK uses two basic functions, a sine and a cosine where as BPSK uses just one .By varying the phase of each of these carriers we can send two bits per each signal. The dimensionality of a modulation is defined by the number of basic functions used. These make QPSK a two –dimensional signal. Not because it sends two bits per symbol, but because it uses two independent signals (a sine and a cosine) to create the symbols. Here are the four symbol mapping definitions for QPSK. Each packet is defined in terms of a sine or a cosine but different phase. (Note that phase is the angle at which signal starts.)

Table- 1 Mapping rule for QPSK

Symbol	Bits	Expression	Phase, (Deg.)	Carrier Signal
S1	00	$\sqrt{\frac{2E_s}{T}} \cos(\omega t + \pi / 4)$	45	
S2	01	$\sqrt{\frac{2E_s}{T}} \sin(\omega t + 3\pi / 4)$	135	
S3	11	$\sqrt{\frac{2E_s}{T}} \cos(\omega t + 3\pi / 4)$	225	
S4	10	$\sqrt{\frac{2E_s}{T}} \sin(\omega t + \pi / 4)$	310	

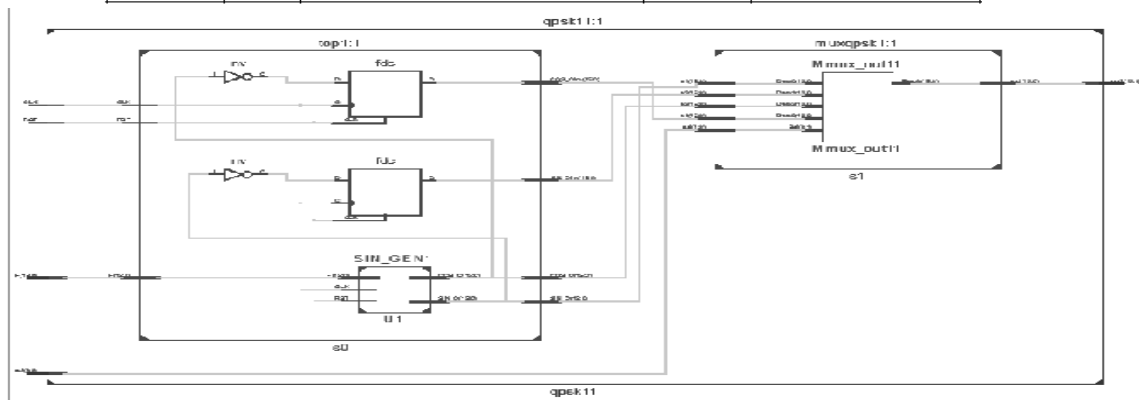


Fig. 11. RTL Schematic for QPSK

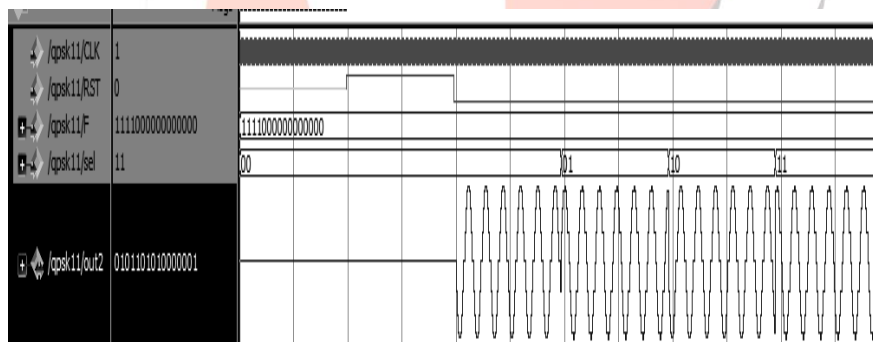


Fig. 12. Simulation result for QPSK

II. DESIGN FLOW

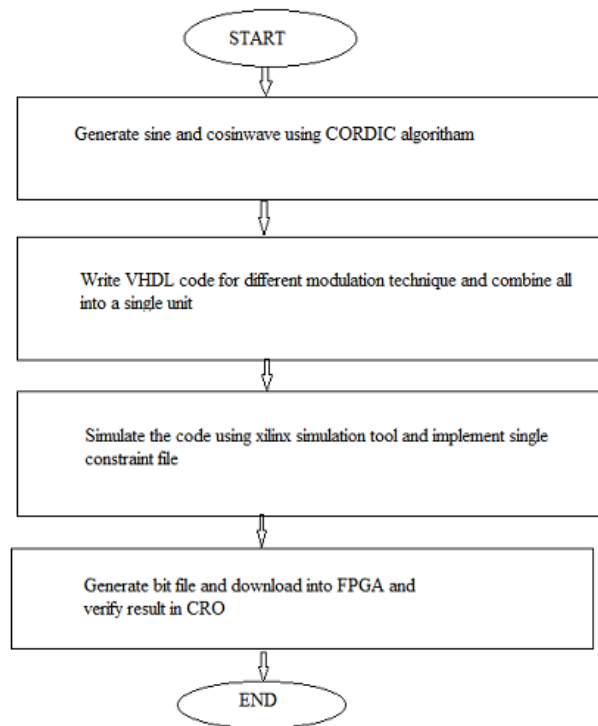


Fig.13. Flow Chart

III. CONTROL UNIT

In control unit, for controlling given data, the multiplexers are used.

Table-2 Control unit information

SL NO	CONTROL BIT	MODE OF OPERATION
1	00	BASK
2	01	BFSK
3	10	BPSK
4	11	QPSK

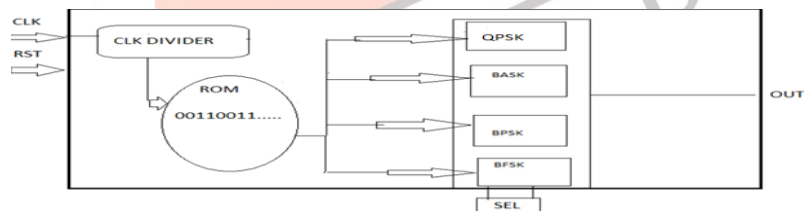


Fig.14. Block diagram of Integrated Digital Modulators

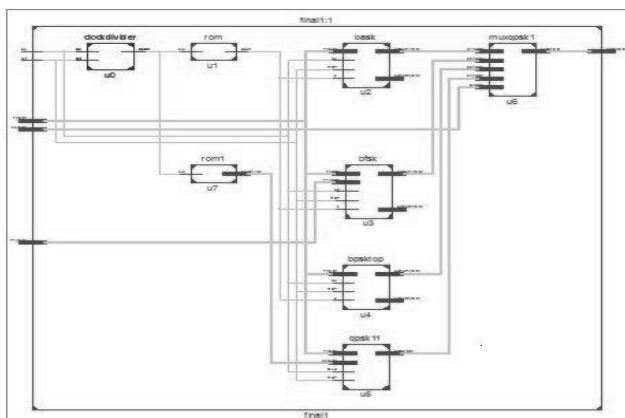


Fig.15. RTL of Integrated Digital Modulators

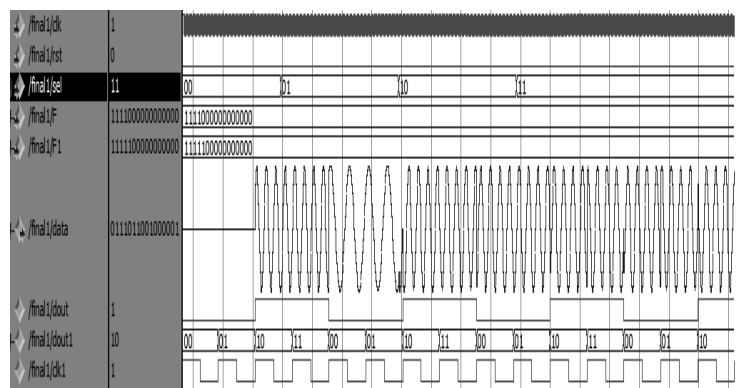


Fig.16. Simulation results of Integrated Digital Modulators

IV .RESULTS AND ANALYSIS

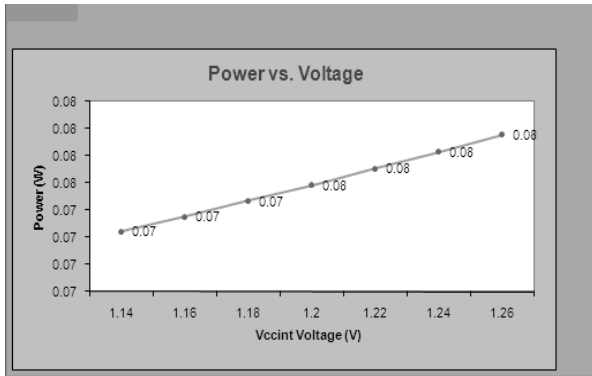


Fig.17. Power Vs Voltage graph for modulation

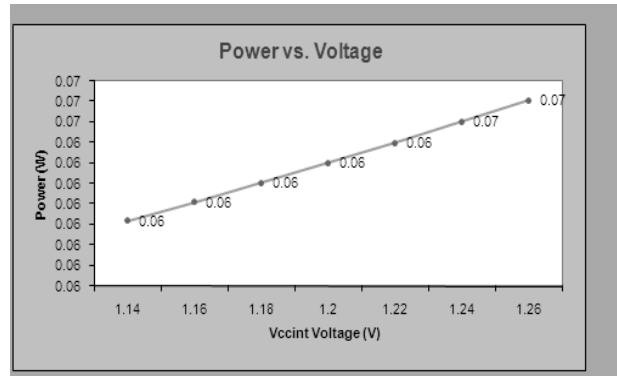


Fig. 18. Power Vs voltage graph for modulation using CORDIC ALGORITHM

Table 3 Power and delay for modulation

POWER(WATTS)	0.063
DELAY(ns)	11.860

Table. 4. Power and delay for modulation using CORDIC algorithm

POWER(WATTS)	0.076
DELAY(ns)	10.928

IV. CONCLUSION

FPGA implementation of BASK, BPSK, BFSK, and QPSK modulators were implemented. The main advantage of this proposed method is the integration of all the basic digital modulators in a single module and can generate carrier signal using CORDIC algorithm thereby avoiding hardware multipliers which are the major power consuming element in digital design.

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