

Optimization of shrinkage in injection-molding of 40% glass filled nylon 66 using response surface methodology (RSM) and genetic algorithm (GA)

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Abstract - In plastic injection molding, process parameters play a major role in the product quality. The values of process parameters depend on various things like, type of plastics, the dimension of the object, dimensional tolerance, etc., so there is no set values and formula of different process parameters. Two-stage optimization technique, response surface methodology (RSM) and genetic algorithm (GA) used to analyze and optimizing a product, for improving its quality by reducing shrinkage. First with the help of literature survey, find most significant process parameters which profoundly influence the shrinkage, also their level. The level also affected by the type of plastics and injection machine. After that with the help of design of experiment (DOE) tool which is part of RSM, develop a sequence of experiment and perform them. RSM gives an analysis of variance (ANOVA) table, after removing insignificant terms from the quadratic model, got equation. This equation is used in GA, and GA gives best possible values of process parameters to minimize the shrinkage. So after optimization, optimized values of process parameters are Mold temperature (M_T) 106.18 °C, Packing time (P) 5.16 sec, Packing pressure (P_p) 14.53 MPa, Cooling time (C) 10 sec. Which results in decreasing Shrinkage by 34.783 %.

Key Words – PIM, RSM, GA, Nylon, Shrinkage, Optimization, DOE

I. INTRODUCTION

In plastics injection molding (PIM) there is a requirement of developing more efficient management system which can minimize the deficits in plastic manufacturing. This literature includes information about the injection molding of plastic and their parameters used in the previous studies. As a result, optimization of the parameters in PIM is important regarding minimizing shrinkage. Minimizing the parameters is not a new concept, but the parameters are different for different machines and products, so it is required to figure out optimality of them every time. Therefore, in this manner, some of the techniques like RSM, GA and combination of them are used to minimize failures in plastics.

Injection molding is widely used to make plastic parts because this method is low cost, less time consuming, and excellent dimensional tolerance. Moreover, there are some more advantages are their like light weight of part and high finish of surface of injection part, which make this process more superior than other. Besides this, plastic injection molding is a very complex process. One of the followings can increase defects in an object like improper mold design, inappropriate material selection and most important improper selection of process parameters. [1][2][3]

The object design and mold design both are mainly done at initial stages of product development, which cannot easily and directly change. So the proper selection of process parameters is the only method to decrease defects and increase quality. [4]

In today's production system 30% of plastic parts are made by plastic injection molding. Proper selection of process parameters is called as "Black Art" because it depends on upon experience and previous knowledge of machine operator and includes a trial-and-error process. Many researchers are working on it to eliminate the costly trial-and-error method by various techniques. [5][3]

In injection molding process there are mainly three stages: filling phase (packing phase), cooling phase and ejection phase. Cooling phase influences productivity and quality of the product. In injection molding, there are many process parameters which depend on and controlled by the machine of plastic injection molding. [6]

At time of manufacturing, quality terms of object such as shrinkages such as shrinkage, warpage, weld lines, mold lines, flow marks, flash marks, sink marks, and void depend on upon process parameters which include Melt temperature, Mold temperature, Injection pressure, Cooling time, Cooling temperature, Screw speed, Packing pressure, Packing time, Cycle time, Fill time, Injection speed [7][8]. Plastic injection molding is one of the important net-shape-forming processes for plastic material like thermoplastics. During this process some defect may occur like: Warpage, Sink marks, Shrinkage, Air traps or voids, Weld lines, Mold lines, Flow marks, Flash marks. However, all defects can avoid and removed by proper selection and optimization of process parameters [9].

Different researchers apply various methods for optimization. Reddy et al. [7] had applied mold flow simulation software and ANN for prediction of warpage in plastic injection molded part. This study proposed further extension by considering number process parameters and output characteristics. Kamaruddin et al. [8] focused only on Taguchi method and target on bending deflection of the plastic tray. The L_9 OA with three levels of four process parameters used. In this study melting temperature, injection speed, cooling time, and holding pressure investigated. The result shows holding pressure was the main contribution of all parameters.

Several studies expose that combination of different optimization techniques; will give improved results in injection molding. This combination of techniques called as hybrid optimization system; firstly it was used by Babur Ozcelik and Tuncay Erzurumlu [10] in 2005. They used a combination of response surface method and genetic algorithm to find the effect of dimensional parameters on warpage. Since each technique has own advantages and disadvantages, so a hybrid technique is a good way to

conquer this difficulty by allowing the benefits of each technique and to discard their weaknesses. However, the best result can only be attained by picking the right process parameters. In previous studies, researchers combined many optimization techniques such as Taguchi, RSM, GA, PSO, SA, and others to improve the quality of the plastic product.

II. EXPERIMENTAL SET-UP

Material, Specimen and Mold Preparation

The size of this product is 235×24×67 (L×W×H×) in mm; the wall thickness is 3 mm as shown in Fig 1 **Error! Reference source not found.**



Fig 1 Product Views

The plastics used in this product is a commonly and commercially used grade of 40% Glass Filled Nylon 66 [11][12], and its material properties listed in Table 1. The technical details of injection molding machine are in Table 1.

Table 1 Properties of Nylon with 44% Glass Filled

THERMAL PROPERTIES	UNIT (METRIC)
Melting Point	263.0 °C
Deflection Temperature at 1.8 MPa (264 psi)	255 °C
PROCESSING PROPERTIES	UNIT (METRIC)
Feed Temperature	260 - 270 °C
Middle Barrel Temperature	270 - 280 °C
Front Barrel Temperature	280 - 290 °C
Nozzle Temperature	271 - 279 °C
Melt Temperature	270 - 300 °C
Mold Temperature	80.0 - 120 °C
Drying Temperature	80.0 °C
Dry Time	3 - 4 hour
Moisture Content	<= 0.20 %
Fill Speed	200 - 300 mm/sec

A JIT 80 SV fully electric horizontal-plastic-injection machine which used as the experimental machine in this experiment is shown in Fig 2 (A).



Fig 2 (A) J.I.T. Injection Molding Machine (B) Shrinkage measurement with help of vernier height gauge

Machining Performances and Evaluation

The machining output in terms product indicated by the shrinkage. In this experiment, the values of shrinkages are examined by using the given formula:

$$S = \frac{L_{cavity} - L_{part}}{L_{cavity}} \times 100 \% \dots\dots\dots Eq 1.$$

Where,

L_{cavity} = inner total length of the cavity and L_{part} = total length of the out came product.

The measurement along with the long length is taken here by using a “vernier height gauge” with *least count* 0.02 mm as shown in Fig 2 (B).

Selection of Machining Parameter and Plan of Experiment

The selected factors for machining parameter and the factorial levels taken from the processing guides of Nylon 66 with 40% Glass Filled material [11][12] and the linked processing parameters according to mechanical equipment used. For optimization of shrinkage and warpage, this study is focused mainly on the influences of the machining parameter in the packing stage. From the literature review, there are four machining parameters which largely influence shrinkage; these are mold temperature (M_T), packing time (P_t), packing pressure (P_p) and cooling time (C_t) in the packing stage. Table 2 shows the levels of four machining parameters.

Table 2 Design scheme and levels machining parameters

SYMBOL	FACTOR	UNIT	LEVELS	
			LOW (-1)	HIGH (+1)
A	Mold temperature (M_T)	°C	80	120
B	Packing time (P_t)	Sec	3	6
C	Packing pressure (P_p)	MPa	10	15
D	Cooling time (C_t)	Sec	8	12

The experimental plan is generated using the predetermined order based on the face-centered CCD and which involves different 30 runs as shown in **Error! Reference source not found.** 3 and value of shrinkage after experiment. Each run will be repeated three times with the same conditions at the different period to get a more precise result in this method.

Table 3 Result of Machine performance evaluation of Shrinkage

	Factor 1	Factor 2	Factor 3	Factor 4	Response
Std	A:Mold Temp.	B:Packing Time	C:Packing Press.	D:Cooling Time	Shrinkage
	C	Sec	MPa	Sec	%
1	80.00	3.00	10.00	8.00	5.2195
2	120.00	3.00	10.00	8.00	3.74429
3	80.00	6.00	10.00	8.00	5.12429
4	120.00	6.00	10.00	8.00	3.43233
5	80.00	3.00	15.00	8.00	2.45613
6	120.00	3.00	15.00	8.00	1.77167
7	80.00	6.00	15.00	8.00	2.04067
8	120.00	6.00	15.00	8.00	1.13946
9	80.00	3.00	10.00	12.00	4.47629
10	120.00	3.00	10.00	12.00	3.51433
11	80.00	6.00	10.00	12.00	4.29333
12	120.00	6.00	10.00	12.00	3.11463
13	80.00	3.00	15.00	12.00	1.88167
14	120.00	3.00	15.00	12.00	1.71046
15	80.00	6.00	15.00	12.00	1.37846
16	120.00	6.00	15.00	12.00	1.11

	Factor 1	Factor 2	Factor 3	Factor 4	Response
Std	A:Mold Temp.	B:Packing Time	C:Packing Press.	D:Cooling Time	Shrinkage
	C	Sec	MPa	Sec	%
17	60.00	4.50	12.50	10.00	4.01271
18	140.00	4.50	12.50	10.00	2.14954
19	100.00	1.50	12.50	10.00	3.37171
20	100.00	7.50	12.50	10.00	2.55654
21	100.00	4.50	7.50	10.00	5.12087
22	100.00	4.50	17.50	10.00	1.23338
23	100.00	4.50	12.50	6.00	3.29571
24	100.00	4.50	12.50	14.00	2.40354
25	100.00	4.50	12.50	10.00	2.76533
26	100.00	4.50	12.50	10.00	2.76533
27	100.00	4.50	12.50	10.00	2.76533
28	100.00	4.50	12.50	10.00	2.76533
29	100.00	4.50	12.50	10.00	2.76533
30	100.00	4.50	12.50	10.00	2.76533

III. RESULTS AND DISCUSSION

ANOVA analysis of shrinkage

The results of the quadratic model for the shrinkage in the form of ANOVA presented in table 4. The value of Probability of F in table 4 for this model is less than 0.05 (i.e. $\alpha=0.05$, or 95% confidence) indicates that the model is considered to be statistically significant, which is wanted as it shows that the conditions in the model have a significant result on the shrinkage. The Model F-value of 107.55 shows the model is great. There is only a 0.01% possibility that an F-value this large might happen due to noise. A value of Probability of F is less than 0.0500 shows that model terms are significant. In this study, A, B, C, D, AC, AD, C² are significant model terms. The remaining terms have not considerable effect because their Probability of F is greater than 0.05. These non-considerable terms can remove, and the analysis of lack-of-fit as well displays as insignificant.

From Table 5 the Predicted R² of 0.9432 is in sensible accord with the Adjusted R² of 0.9808; i.e. the difference is less than 0.2. Adequate Precision measures the signal to noise ratio. A ratio must be greater than four is wanted. In this experiment ratio is 39.629 indicates a sufficient symbol.

Table 4 Quadratic model for the shrinkage in ANOVA (before elimination)

Source	Sum of Squares	df	Mean Square	F Value	p-value Prob > F	
Model	39.42	14	2.82	107.55	< 0.0001	significant
A-Mold temp.	5.10	1	5.10	194.65	< 0.0001	
B-Packing Time	0.95	1	0.95	36.23	< 0.0001	
C-Packing Press.	30.84	1	30.84	1177.84	< 0.0001	
D-Cooling time	1.14	1	1.14	43.59	< 0.0001	
AB	0.035	1	0.035	1.33	0.2662	
AC	0.67	1	0.67	25.72	0.0001	
AD	0.29	1	0.29	11.27	0.0043	
BC	0.084	1	0.084	3.22	0.0929	
BD	3.350E-003	1	3.350E-003	0.13	0.7256	
CD	0.039	1	0.039	1.51	0.2385	
A ²	0.097	1	0.097	3.69	0.0739	
B ²	0.025	1	0.025	0.95	0.3452	
C ²	0.19	1	0.19	7.28	0.0165	
D ²	6.044E-005	1	6.044E-005	2.308E-003	0.9623	
Residual	0.39	15	0.026			
Lack of Fit	0.39	10	0.039	0	0	Non-significant
Pure Error	0.000	5	0.000			
Cor Total	39.82	29				

Table 5 R² for the response – shrinkage (before elimination)

Std. Dev.	0.16	R ²	0.9901
Mean	2.90	Adjusted R ²	0.9808
Coefficient of Variation	5.57	Predicted R ²	0.9432
PRESS	2.26	Adequate Precision	39.629

With the help of backward elimination process, it eliminates the unimportant terms to correct the quadratic model of shrinkage. The new result of ANOVA table after removing non-considerable terms for the shrinkage presented in Table 6. The compact model results expose that this model is still significant in the rank of the value of Probability of F is less than 0.05, and the check of lack-of-fit is as well insignificant because the Probability of F value greater than 0.05. The additional key coefficient R^2 in the resulting ANOVA table explains the ratio of the explain variation to the total variation. It is a shows the degree of fit.

Table 6 Modified model for the shrinkage in ANOVA (after backward elimination)

Source	Sum of Squares	Df	Mean Square	F Value	p-value Prob > F	
Model	39.15	7	5.59	184.41	< 0.0001	Significant
A-Mold temp.	5.10	1	5.10	168.04	< 0.0001	
B-Packing Time	0.95	1	0.95	31.28	< 0.0001	
C-Packing Press.	30.84	1	30.84	1016.87	< 0.0001	
D-Cooling time	1.14	1	1.14	37.63	< 0.0001	
AC	0.67	1	0.67	22.21	0.0001	
AD	0.29	1	0.29	9.73	0.0050	
C²	0.15	1	0.15	5.10	0.0342	
Residual	0.67	22	0.030			
Lack of Fit	0.67	17	0.039	0	0	Non-significant
Pure Error	0.000	5	0.000			
Cor Total	39.82	29				

As we when R^2 approaches unity; the response model fits the Actual data much better. The value of R^2 shown in Table 7, for reduced model this value is over 0.95, which is reasonably near to unity, which one acceptably good. It means that the new model explains about 95% of the unpredictability (variability) in the data. It also verifies that this model presents a brilliant justification to the relationship between the independent factors and the response (shrinkage). The Predicted R^2 of 0.9518 is in reasonable concord with the Adjusted R^2 of 0.9789; because the difference between them is less than 0.2. As we know that ratio must be greater than four is wanted, in our experiment ratio is 50.422, which indicates an enough signal.

Table 7 R^2 for the response – shrinkage (after backward elimination)

Std. Dev.	0.17	R²	0.9835
Mean	2.90	Adjusted R²	0.9789
Coefficient of Variation	6.10	Predicted R²	0.9518
PRESS	1.96	Adequate Precision	50.422

Shrinkage Optimization by Genetic Algorithm

The optimal process for machining the 40% Glass Filled Nylon 66 with the constraints of machining parameters range is to find the optimal values of machining parameters (X) to minimize the amount of shrinkage during the plastic injection molding process. The optimization problem can be approximated by the following Eq and then solved using a GA method on MATLAB Software.

Find $X = [M_T; P_i; P_p; C_t]$

to minimize $f(X) = S$

Subject to $80 < M_T < 120$ °C, $3 < P_i < 6$ sec, $10 < P_p < 15$ MPa, $9 < C_t < 12$ sec

The feasible ranges of M_T , P_i , P_p and C_t have been selected based on the recommended value in the processing guides of material used (40% Glass Filled Nylon 66).

$$\text{Shrinkage} = +22.85958 - 0.10828 * x(1) - 0.13254 * x(2) - 1.15675 * x(3) - 0.44848 * x(4) + 4.10313e-003 * x(1) * x(3) + 3.39453e-003 * x(1) * x(4) + 0.011721 * x(3)^2 \dots \text{Eq 2}$$

The considerable parameters of genetic algorithm in solve an optimization problem in effect way are the mutation rate, the size of the population, the number of iterations (generations), etc. In this model, the population size of 15*no. of variables (60), a crossover rate of 1.0, the mutation rate of 0.2, bit number for each variable of 16, and a number of generations 800 employed. Table 8 presents the results obtained from the four machining parameters with the optimum adjustments found by the GA. As shown in Table 8, the optimized shrinkage S of 1.80% represents a reduction of 34.783% compared to the initial shrinkage S of 2.76%.

Table 8 The comparison between initial value and optimal value

Parameters	Unit	Initial value	Optimal value	Optimal value	% reduction
Mold temperature (M_T)	°c	100		106.18	
Packing time (P_t)	Sec	4.5		5.16	
Packing pressure (P_p)	MPa	12.5		14.53	
Cooling time (C_t)	Sec	10		10	
Shrinkage (S)	%	2.76		1.80	34.783 %

IV. CONCLUSIONS

The conclusions of the research are as follows:

1. The results of ANOVA and performance explain that the quadratic models of the shrinkage are quite well fit through the experimental values. It has analyzed that controls of all the process parameters on the performance of shrinkage by the getting mathematical models.

2. The value of shrinkage increases as the mold temperature increases. The sufficient time of cooling and packing is beneficial for minimizing the amount of shrinkage. The proper setting of packing pressure and packing time can provide enough melt volume in the packing stage and can diminish the phenomenon of shrinkage.

3. The four machining parameters with the optimum adjustment obtained by using the GA. For the manufacture of 40% Glass Filled Nylon 66 product, the optimal values of shrinkage represent a reduction of 34.783 after this process.

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