

Simulation of Security Constraint Optimal Power Flow Using Power World Simulator

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Abstract— This paper presents an efficient approach to find Security Constraint Optimal Power Flow (SCOPF) determining the dispatch schedule of power generators with minimum cost. Satisfying system constraints, transmission constraints along with mandates to ensure optimal power flow has led to SCOPF. Revenue paid for electricity will be reduced considerably while the generation cost is reduced. Power world simulator employs linear programming method for finding optimal power flow. The proposed method has been tested and examined on ieee-7 bus system. Results shows advantageous than other conventional methods for solving OPF with security constraint for the same case.

Index Terms—Power World Simulator, Optimal power Flow, security Constraint Optimal Power Flow, Economic Dispatch

I. INTRODUCTION

In power systems, operation and planning needs operators to make decisions with respect to different objectives. Several tools have been developed to assist operators in this aspect. Optimal Power Flow (OPF) is one of them which help the operators in running the system optimally under specific constraints. Operating power systems at minimum cost without maintaining the security is no longer the sufficient criterion for dispatching electric power and therefore suitable control measures should be made. This has led to Security Constraint Optimal Power Flow. As the power industry moves into a more competitive environment, use of Optimal Power Flow will become increasingly more important in maximizing the capability of the existing transmission system asset. A typical OPF solution adjusting the appropriate control variables, so that a specific objective in operating a power system network is optimized (maximizing or minimizing) with respect to the power system constraints, dictated by the electrical network and with security constraints is solved in this paper. Security constrained optimal power flow takes into account outages of certain transmission lines or equipment. A SCOPF solution is secure for all credible contingencies or can be made secure by corrective means. Due to the computational complexity of the problem, more work has been devoted to obtaining faster solutions requiring less storage. Several classical methods has been used in solving OPF for decades and here one of it ,linear programming is used to find the optimal solution for this problem as it is the fast method among the classical methods for solving SCOPF.

II. PROBLEM FORMULATION

The optimal power flow is a constrained optimization problem requiring the minimization of:

$$F=(x,u)$$

Subject to constraints

$$G_i(x, u) = 0, i=0, 1, 2, 3 \dots m \text{ (equality constraints)}$$

$$H_i(x, u) \leq 0, i=0, 1, 2, 3 \dots m \text{ (inequality constraints)}$$

$$u^{\min} \leq u \leq u^{\max}$$

$$x^{\min} \leq x \leq x^{\max}$$

Here

$f(x,u)$ is the scalar objective function,

$g(x,u)$ represents nonlinear equality constraints (power flow equations),

$h(x,u)$ is the nonlinear inequality constraints.

u and x represents set of controllable and dependent variables respectively.

The Vector X Contains Dependent Variables Consisting Of Bus Voltage Magnitudes And Phase Angles, As Well As The Mvar Output Of Generators Designated For Bus Voltage Control And Fixed Parameters Such As The Reference Bus Angle, Non-Controlled Generator Mw And Mvar Outputs, Non-Controlled Mw And Mvar Loads, Fixed Bus Voltages, Line Parameters, etc.

A. Objective function

In the solution of SCOPF, the main objective is to minimize total operating costs of the system with maintaining the system security. In OPF, when the load is light, the cheapest generators are always the ones chosen to run first. As the load increases, more and more expensive generators will then be brought in. Thus, the operating cost plays a very important role in the solution of OPF. The amount of fuel or input to a generator is usually expressed in Btu/hr (British Thermal units per hour) and its output in MW (Mega Watts).Figure 1 shows a typical input-output curve of a generator (slack bus generator) also commonly known as the heat-rate curve.

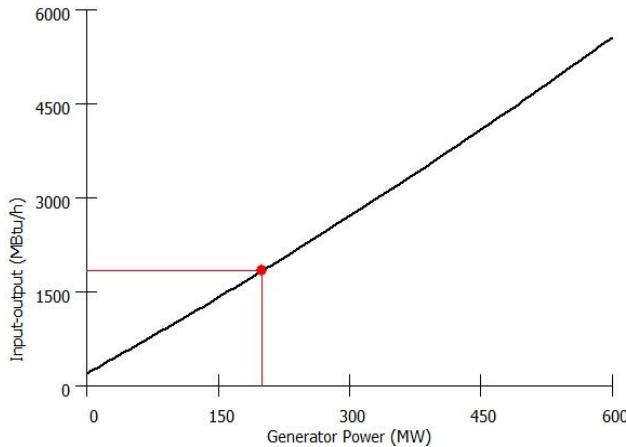
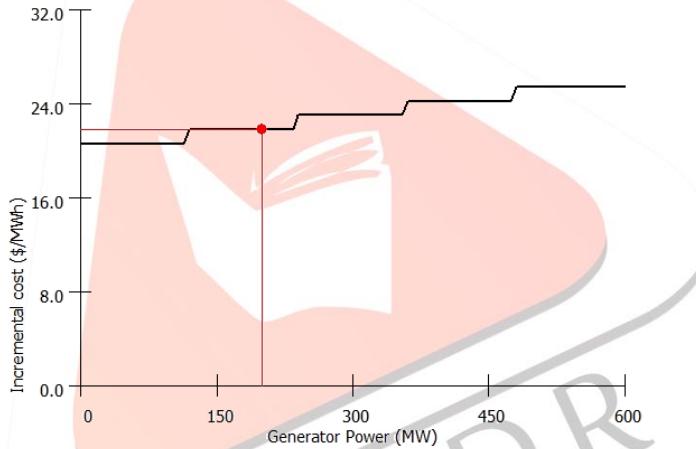


Figure 1: Typical Input-output Curve of a Generator

It specifies the relationship between how much heat must be input to the generator and its resulting MW output. In all practical cases, the cost of generator i can be represented as

$$C_i = (a_i + b_i P_i + c_i P_i^2) * \text{fuel cost}$$

Where P_i is the real power output of generator i , and a_i, b_i, c_i are the cost coefficients.



Typical incremental cost curve is shown below in figure 2

B. Control Variables

The control variables in an optimal power flow problem are the quantities whose value can be adjusted directly to help minimize the objective function and satisfy the constraints. The control variables can be given as:

1. Real power and reactive power generation.
2. Phase-shifter angles
3. Net interchange
4. Load MW and MVar (load shedding)
5. DC transmission line flows
6. Control voltage settings
7. LTC transformer tap settings

C. Dependent Variables

These variables are the optimal power flow variables that are not controlled. These include all type of variables that are free, within limits, to assume value to solve the problem. The main dependent variables are complex bus voltage angles and magnitude.

D. Constraints

Constraints are the operating limits to the problem. In a conventional power flow, equipment limits are normally supplied by the user for monitoring purposes, such as printing out of any violations of circuit flow limits. Only the power flow algorithm enforces a small set of limits, such as, tap limits and generator MVAR limits. In contrast, an OPF enforces all equipment limits input by the user. This may easily lead to problem infeasibility if the limits are too restrictive or inconsistent. Careless input of limits should therefore be avoided.

A commercially available OPF normally offers a facility to relax limits in case of unfeasibility. Once a solution is obtained for the relaxed problem, the OPF will provide means to investigate how the original limits had caused convergence difficulties. Such a mechanism may provide valuable information concerning the power system being modelled. For instance, a region which requires relaxation of voltage limits may have implications of requiring new reactive compensation sources.

Some OPF programs require users to give them guidance as to which limits can be relaxed and in what sequence. This flexibility in fact places much burden on the users who need to appreciate how an OPF algorithm performs before the preferred strategy for constraint relaxation can be formalized as input to the program.

E. Equality constraint

The equality constraints of the OPF reflect the physics of the power system as well as the desired voltage set points throughout the system. The physics of the power system are enforced through the power flow equations which require that the net injection of real and reactive power at each bus sum to zero. This can be achieved by active and reactive power analysis

$$P_i = P \text{ Load} + P \text{ Loss}$$

$$Q_i = Q \text{ Load} + Q \text{ Loss}$$

Where

P_i & Q_i are the active and reactive power outputs.

$P \text{ Load}$ & $Q \text{ Load}$ is the active and reactive load power.

$P \text{ Loss}$ & $Q \text{ Loss}$ is the active and reactive power loss.

The power flow equations of the network can be given as:

$$G(V, \delta) = 0$$

Where

$P_i(V, \delta) - P_i \text{ net}$

$G(V, \delta) = \{Q_i(V, \delta) - Q_i \text{ net}$

$P_m(V, \delta) - P_m \text{ net}$

P_i & Q_i are the calculated real and reactive power at PQ bus

V & δ are the magnitude and phase angle of voltage at different buses.

G. Inequality Constraints.

In a power system components and devices have operating limits & these limits are created for security constraints. Thus the required objective function can be minimized by maintaining the network components within the security limits.

$$P_{gi} \text{ min} \leq P_{gi} \leq P_{gi} \text{ max}$$

$$Q_{gi} \text{ min} \leq Q_{gi} \leq Q_{gi} \text{ max}$$

$$\sum P_{gi} - PD - PLoss = 0$$

Where

P_{gi} is the amount of generation in MW at generator i.

Q_{gi} is the amount of generation in MVAR at generator i.

The inequality constraints on voltage magnitude V of each PQ bus

$$V_i \text{ min} \leq V_i \leq V_i \text{ max}$$

Where

$V_i \text{ min}$ & $V_i \text{ max}$ are the minimum and maximum values of voltages at bus i.

The inequality constraints on phase angle δ of voltages at all buses i

$$\delta_i \text{ min} \leq \delta_i \leq \delta_i \text{ max}$$

Where

$\delta_i \text{ min}$ & $\delta_i \text{ max}$ are the minimum and maximum values of phase angle at bus i

III. AUTOMATIC VOLTAGE CONTROL

Automatic generation control (AGC) is the name given to a control system having three major objectives:

1. To hold system frequency at or very close to a specified nominal value
2. To maintain the correct value of interchange power between control
3. To maintain each unit's generation at the most economic value.

Modern implementation of automatic generation control (AGC) schemes usually consists of a central location where information pertaining to the system is telemetered. Control actions are determined in a digital computer and then transmitted to the generation units via the same telemetry channels. To implement an AGC system, one would require the following information at the control center.

1. Unit megawatt output for each committed unit.
2. Megawatt flow over each tie line to neighboring systems.
3. System frequency.

The output of the execution of an AGC program must be transmitted to each of the generating units. Present practice is to transmit raised or lower pulses of varying lengths to the unit. Control equipment then changes the unit's load reference set point up or down in proportion to the pulse length. The "length" of the control pulse may be encoded in the bits of a digital word that is transmitted over a digital telemetry channel. The use of digital telemetry is becoming commonplace in modern systems wherein supervisory control (opening and closing substation breakers), telemetry information (measurements of MW, MVAR, MVA voltage, etc.) and control information (unit raise/lower) is all sent via the same channels.

IV. SOLVING SCOPF

Before solving for security constraint optimal power flow base case should be solved, this can be either by normal power flow or optimal power flow. Here the initial base case is solved using optimal power flow and then the constraint is added to the base case to solve for SCOPF

V. SIMULATION AND RESULTS

An IEEE 7-bus power system is considered for SCOPF Simulation. For the same bus system OPF and SCOPF is solved .Figure-3 in this paper is from Power World Simulator. IEEE- 7 bus system is divided into three areas. Top area contains generator 1, 2, 3, and left area contains generator 4 and right area contains generator 5.

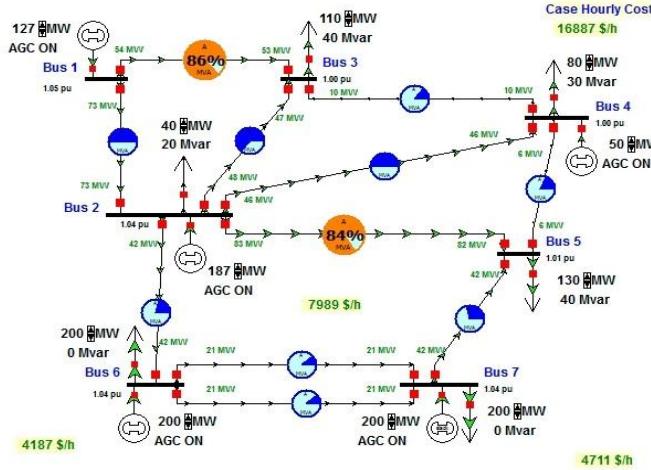


Figure 3: IEEE 7 bus system solved for OPF

Figure 3 shows a 7 bus IEEE system solved for OPF . it can be noted that line from bus 1 to bus 3 and line from bus 2 to bus 5 are loaded 86 % and 84 %. This is a threat to security of the power system as it could reduce the reliability of the transmission system. Thus to ensure security of the system by reducing the burden on the transmission line for the same system, security constraint optimal power flow is solved and the simulation is shown in figure 4 .

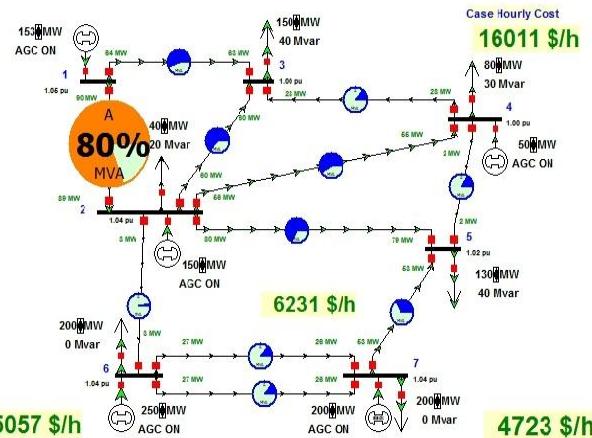


Figure 4: IEEE 7 bus system solved for SCOPF

Figure-5 shows composite incremental cost curve in top area of 7 bus system. For 353 MW of total generation in top area , incremental cost curve is 13 \$/MWhr. Figure-6 shows composite incremental cost curve in left area of 7 bus system. For 200 MW of total generation in left area , incremental cost curve is 17 \$/MWhr. Figure-7 shows composite incremental cost curve in right area of 7 bus system. For 200 MW of total generation in right area , incremental cost curve is 22.5 \$/MWhr.

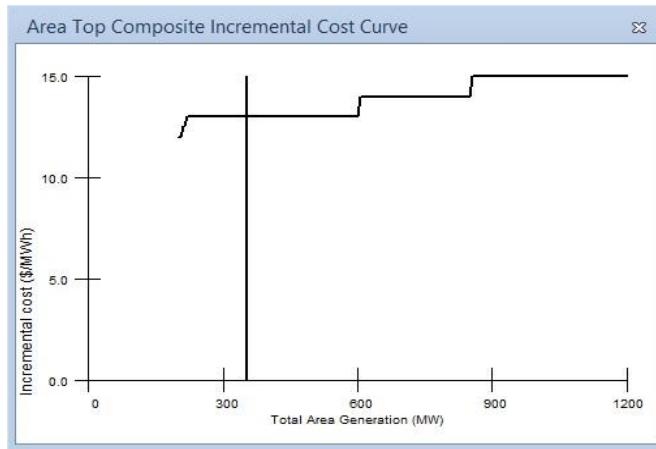


Figure 5: Top Area composite incremental cost curve of 7-bus system.

Figure -8 shows generator 1,2,3 incremental cost curve in top Area in 7 bus system. Figure -8 shows generator 4 incremental cost curve in left area. Figure-11 shows generator 5 incremental cost curve in right area in 7-bus system. The optimum value for operation of generator 4 is at 250 MW with incremental cost of 17.5\$/MWhr. The optimum value for operation of generator 5 is at 200 MW with incremental cost of 22\$/MWhr. The optimal value for operation of generator 1, 2, 3 is at 353 MW with an incremental cost of 13\$/MWhr.

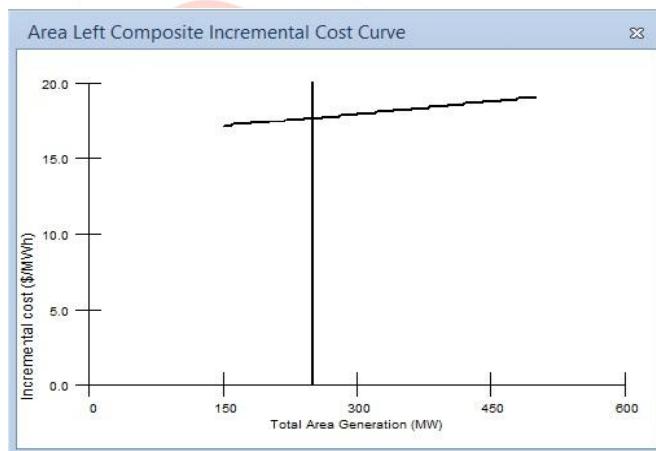


Figure 6: Left area composite incremental cost curve of 7-bus system

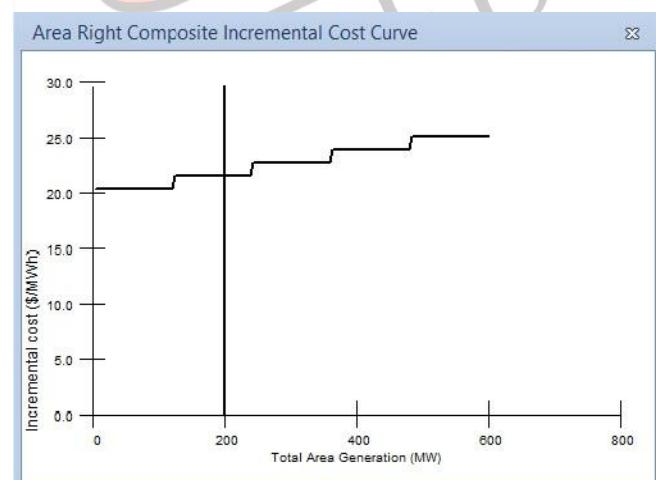


Figure 7: Right area composite incremental cost curve of 7-bus system

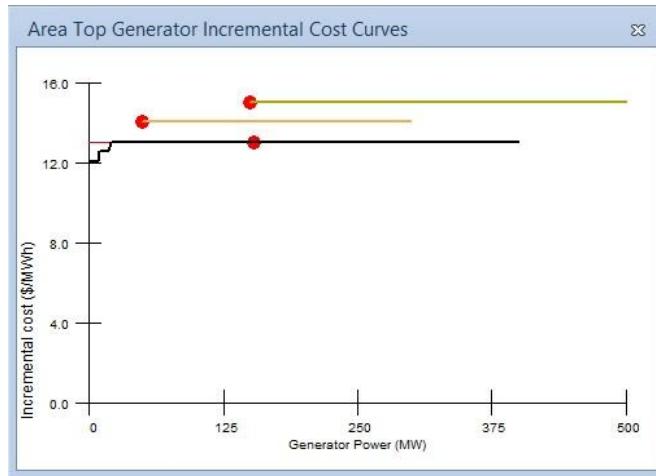


Figure 8: Top Area Generator incremental cost curves of 7 bus system.

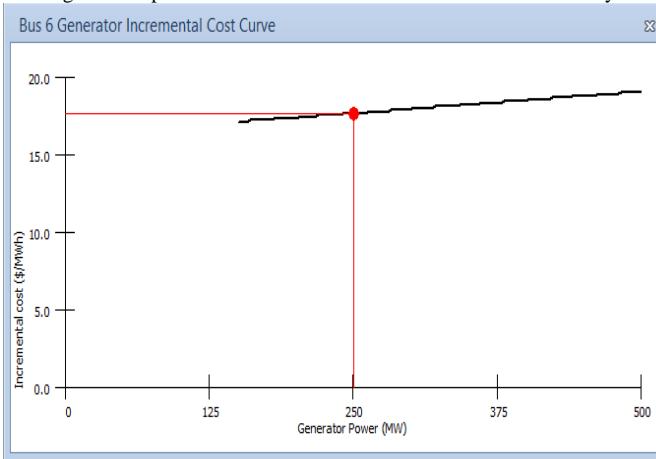


Figure 9: Top Area Generator incremental cost curves of 7 bus system.

Table 1: Showing percentage how transmission line loaded in 7-bus system while solving OPF and SCOPF

Line	Load While Solving OPF	Load While Solving SCOPF
1-2	49.0%	80%
1-3	86.2%	55.4%
2-3	63.6%	63.7%
2-5	83.9%	67.8%
2-6	21.6%	2.1%
3-4	14.5%	12.8%
4-5	18.5%	16.7%
5-7	28.5%	31.6%
6-7(1)	10.9%	13.4%
6-7(2)	10.9%	13.4%

Table 1 shows the difference in percentage of line loading for the 7-bus system while solving OPF and SCOPF. From the table it can be noted that line from bus 1 to bus 3 and line from bus 2 to bus 5 is loaded 86.2% and 83.9% respectively while solving for base OPF. While solving SCOPF for the same case line from bus 1 to bus 2 alone is loaded to 80%.

Table 2 shows difference total fuel cost for various areas in the 7-bus system while solving for OPF and SCOPF. While solving the base case OPF the total cost for the system to generate a power of 803MW is 16887 \$/when SCOPF solved for the same case the total generation cost for generating power of 803 MW is reduced to 16011 \$/h. The top, left and right area cost for the 7-bus system while solving for OPF are 7989 \$/h, 4187 \$/h and 4711 \$/h respectively. The top, left and right area cost for the 7-bus system while solving for SCOPF are 6231 \$/h, 5057 \$/h and 4723 \$/h respectively.

Table 2: Showing the area cost for the system while solving OPF and SCOPF

Area	Cost While Solving OPF (\$/h)	Cost While Solving SCOPF(\$/h)
Top	7989 \$/h	6231 \$/h
Left	4187 \$/h	5057 \$/h
Right	4711 \$/h	4723 \$/h
Total cost	16887 \$/h	16011 \$/h

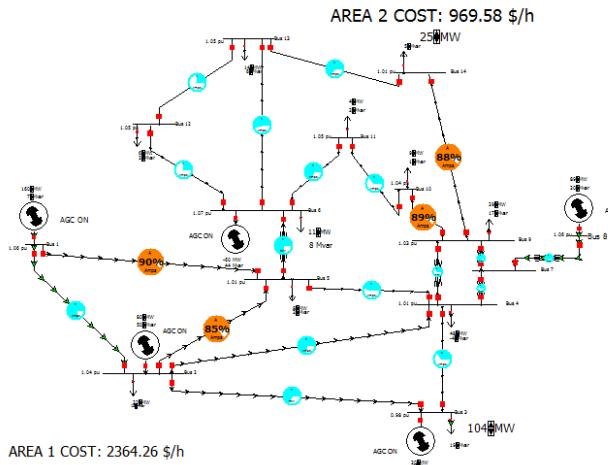


Figure 10: SCOPF solved for IEEE 14 bus system.

Figure 10 shows the simulation of Security Constrained Optimal Power Flow solved for IEEE 14 bus system. The area 1 and area 2 cost of the system is 2364.26 and 969.58 respectively.

VI. DISCUSSIONS

Some comments on proposed approach are as follow:

- Non Linear Programming method is a fast method for solving OPF and provides optimal result in less computation time.
- Power World Simulator employs a Nonlinear programming (NLP) OPF implementation. It determines the optimal solution by iterating between solving a standard power and then solving a linear program to change the system controls to remove any limit violations.
- It is now possible to optimally dispatch the generation in an area or group of areas while simultaneously enforcing the transmission line and interface limits. Simulator OPF can then calculate the marginal price to supply electricity to a bus (also known as the locational marginal price), taking into account transmission system congestion.

VII. CONCLUSIONS

In this work, an attempt is made to find optimum power solution for 7bus system and IEEE-14 bus system. Different objectives are considered to solve the problem and to minimize the cost of operation. The proposed method is used to consider different cases by varying MVAR load and the cost of operation is compared. Larger power systems can be considered in order to obtain more realistic results. Larger systems will allow for better flexibilities in OPF analysis. The SCOPF problem solved using power world simulator has ability to display the SCOPF results on system one-line diagrams and contour the results for ease of interpretation. By solving security constraint OPF the stability and reliability of the system is maintained.

VIII. FUTURE SCOPE

The future scope is to implement this method to large power systems and to introduce FACTS device into the system for reactive power compensation and also to find the optimal location of FACTS devices in to the system.

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